Energy Efficiency Maximization of Backscatter-Assisted Wireless-Powered MEC With User Cooperation

Yejun He, Senior Member, IEEE, Xinying Wu, Zhou He, and Mohsen Guizani, Fellow, IEEE

Abstract—The integrated backscatter communication (BackCom) and active communication (AC) scheme can improve wireless-powered mobile edge computing (WPMEC) system performance in general single-user and multi-user scenarios. However, there is little research in the cooperation-assisted WPMEC scenario. In this article, we consider a cooperation-assisted WPMEC system consisting of a source node (SN), a helper and a hybrid access point (HAP) integrated with MEC servers. An innovative user cooperation (UC) scheme with the integrated BackCom and AC is proposed to enhance the system performance. As a relay, the helper can help the SN to transmit its computing tasks due to the poor communication link between the SN and the HAP. To be specific, we aim at maximizing the user energy efficiency (EE) by jointly optimizing the backscatter reflection coefficient for BackCom, the transmission power for AC, the system time and task optimization allocation while considering the minimum computation bits requirement, the channel capacity and energy constraints. Based on a fractional program, we first transform the EE maximization problem into an equivalent one (non-convex problem) and then transform this non-convex problem into a convex problem by exploiting variable substitution and convex optimization. In addition, semi-closed form expressions of the optimal solution are deduced. An energy efficiency maximization algorithm is proposed to solve this convex problem. Simulation results demonstrate that the proposed scheme significantly improves the user EE than the existing schemes.

Index Terms—Backscatter communication, convex optimization, mobile edge computing (MEC), user cooperation, wireless power transfer (WPT).

I. INTRODUCTION

With the development of communication technology and the Internet of Things (IoT), there are many application scenarios of wireless devices, such as autonomous driving, virtual reality (VR), smart city and tele-surgery [1], where these applications are computation-intensive and latency-sensitive. However, the mobile devices with poor computing capabilities and finite battery capacity may have difficulties in handling massive computational tasks [2]. To deal with this issue, mobile edge computing (MEC) [3], named as a distributed computing method, can sink computing and storage capabilities to the access network close to the users. Wireless devices can offload computation tasks to the nearby MEC servers, thus significantly improving the computation capabilities and help reduce the latency.

However, these wireless devices are equipped with small battery capacities. It is troublesome to constantly replace the batteries of billions of such IoT devices. To solve this problem, wireless power transfer (WPT) [4] has been proposed to provide a sustainable energy supply. In a wireless-powered mobile edge computing (WPMEC) network, a hybrid access point (HAP) [5] broadcasts radio frequency (RF) energy to the wireless devices. By energy harvesting (EH) technology [6], the users can convert the received RF signals to charge battery. Relying on the harvested energy, users can accomplish the computation tasks by local computing and offloading to MEC servers.

Extensive studies have investigated the WPMEC [7], [8]. In an updated work [9], the authors minimized the delay by online learning while considering the task deadline and energy constraints. Wang et al. [10] investigated how to provide personalized services by various unmanned aerial vehicle (UAV) owners. In addition, a dynamic scenario containing multi-user and multi-UAV integrated with the MEC server was considered in [11] to minimize the total computation cost. However, there exists a double near-far effect in these systems [12]. A remote user harvests less energy, but needs to consume much energy for task offloading [13]. To address this issue, a user cooperation (UC) scheme [14] is an effective way to improve the system performance. In this UC scheme, the near user acts as a relay to transmit the signal of the far user. In [15], the authors discussed a basic UC scheme. Due to the terrible communication channel between one user and the MEC servers, task offloading needs the help of another user. The authors maximized the total throughput by jointly optimizing the local computing frequency, the transmit power, the task and the time allocation.

Recently, Backscatter Communication (BackCom) [16], [17] has received significant attention. In BackCom [18], [19], the...
transmitter works in a full duplex mode. Specifically, it can operate in passive mode by modulating and reflecting the incident signal to the receiver without generating a carrier frequency, while harvesting energy to support circuit consumption [20], [21]. As for traditional active communication (AC), the transmitter first harvests energy and then uses the harvested energy to transfer data, which is based on harvest-then-transmit (HTT) protocol. Generally, the AC mode consumes more energy than BackCom while achieving a higher transfer rate. There is a tradeoff between the EH and the data transfer for BackCom and AC, so they can be combined to increase the throughput and energy efficiency (EE) [22], [23].

In [24], the weighted sum computation bits maximization problem was studied in WPMEC with integrated BackCom and AC, where a scenario with power beacon (PB), a MEC server and multiple users were considered. The authors obtained the optimal solution by jointly optimizing the BackCom reflection coefficient and time, the AC power and time, the local computing frequency and the execution time. As for the same system mode, the authors in [25] considered a computational EE fairness problem, which is a non-convex fractional optimization problem. A Dinkelbach-based iterative algorithm was used to obtain the optimal solutions. The EE maximization of all users was investigated in [26], where the authors found the tradeoff between the BackCom and the HTT mode. In [27], the authors jointly considered limited MEC computing capacity, quality of service and energy causal constraints for each user. To maximize the system computing rate and the system EE, a novel two-layer iterative algorithm and a low-complexity algorithm are proposed.

Although the above studies have made some contributions on the general WPMEC system and the backscatter-assisted WPMEC system, there are few existing studies on the cooperation-assisted WPMEC system with the integrated BackCom and AC. Motivated by above observations, we investigate a WPMEC system based on UC consisting of a HAP, a SN and a helper. The BackCom and the AC are allowed to offload the computation tasks. Unlike the system EE considered in [27], [28], in this article, we provide user EE$^1$ maximization algorithm and use convex optimization techniques [30] to obtain an optimal solution of this problem. Simulation results demonstrate that the proposed design significantly improves the user EE, compared with some conventional schemes. Our main contributions are summarized as follows.

1) Improving the computation performance of the WPMEC system. Users can use the integrated BackCom and AC to offload computation tasks. On the UC, the near user can act as a relay to help the edge-cell user to transform data. We aim at maximizing

$^1$Different from the system-centric EE, the user-centric computing EE should not include the energy consumption of HAP. There are some concerns in the system-centric EE maximization. Only users with better energy utilization than the system itself are scheduled, while other users keep silent in this process [29]. As a result, their quality of service cannot be guaranteed. In addition, in WPMEC, the users’ energy comes entirely from the HAP, and this part is less and needs to be fully utilized. HAP is directly connected to the power supply, so the system-centric EE optimal solution is not optimal for each user. The user-centric EE pays attention to the users’ energy efficiency, which is more consistent with the actual application scenarios.

2) Applying a fractional program, variable substitution and Lagrange method to transform the non-convex fractional problem to a convex problem and deduce semi-closed form expressions of the optimal solutions.

3) Proposing an energy efficiency maximization algorithm to solve this convex optimization problem. Our algorithm is computation-efficient and the proposed scheme significantly improves the user EE than the existing schemes.

The remainder is organized as follows. Section II presents the cooperation-assisted WPMEC system with the integrated BackCom and AC, including the communication model, the integrated backCom and AC protocol in the UC scenario and the computation model. Section III introduces the EE maximization problem, the energy efficiency maximization algorithm and the optimal solution of this problem. Simulation results are presented in Section IV. The last section gives the conclusion of this work.

II. SYSTEM MODEL

A. Communication Model

We consider a user-cooperation WPMEC scenario as illustrated in Fig. 1, including two users and a HAP. One user far away from the HAP, called source node (SN), has a large number of computation tasks. Another user near to the HAP in an idle state is called helper. The HAP can provide the wireless energy and the task offloading for users, and these users can convert the received RF signals to charge the battery. Moreover, a partial offloading is adopted and computation tasks can be executed at the SN, the helper and the HAP in parallel. Due to the terrible channel condition between the SN and the HAP, the SN can offload tasks to helper and HAP with the aid of the helper by the UC. The helper can perform part of the tasks locally, and further offload the remaining tasks to the HAP. After the HAP completes
TABLE I
KEY NOTATIONS

<table>
<thead>
<tr>
<th>Notation</th>
<th>Definition</th>
</tr>
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<tbody>
<tr>
<td>$T$</td>
<td>The time block</td>
</tr>
<tr>
<td>$t_{b,0}^{s, h}$</td>
<td>The time for the BackCom</td>
</tr>
<tr>
<td>$t_{a,0}^{s, h}$</td>
<td>The time for the AC</td>
</tr>
<tr>
<td>$t_{ac}^{s}$</td>
<td>The number of tasks executed by the SN locally</td>
</tr>
<tr>
<td>$l_{b}^{h}$</td>
<td>The number of tasks offloaded to the helper by the BackCom</td>
</tr>
<tr>
<td>$l_{a}^{p}$</td>
<td>The number of tasks offloaded to the helper by the AC</td>
</tr>
<tr>
<td>$l_{b}^{p}$</td>
<td>The number of tasks offloaded to the HAP by the BackCom</td>
</tr>
<tr>
<td>$l_{a}^{p}$</td>
<td>The number of tasks offloaded to the HAP by the AC</td>
</tr>
<tr>
<td>$P_0$</td>
<td>The power of the HAP</td>
</tr>
<tr>
<td>$\mu$</td>
<td>The energy conversion efficiency</td>
</tr>
<tr>
<td>$\kappa$</td>
<td>The equal computing efficiency parameter</td>
</tr>
<tr>
<td>$h_{s, h, 0}$</td>
<td>The channel gain</td>
</tr>
<tr>
<td>$f_s, f_h$</td>
<td>The CPU frequency</td>
</tr>
<tr>
<td>$\phi_s, \phi_h$</td>
<td>The CPU cycles required to compute 1 bit task</td>
</tr>
<tr>
<td>$\beta_s, \beta_h$</td>
<td>The reflection coefficient of the BackCom</td>
</tr>
<tr>
<td>$p_s, p_h$</td>
<td>The power of the AC</td>
</tr>
<tr>
<td>$\sigma^2$</td>
<td>The noise power</td>
</tr>
<tr>
<td>$W$</td>
<td>The system bandwidth</td>
</tr>
<tr>
<td>$p_{bac}, p_{bac}$</td>
<td>The circuit consumption of the BackCom</td>
</tr>
<tr>
<td>$p_{act}, p_{act}$</td>
<td>The circuit consumption of the AC</td>
</tr>
<tr>
<td>$L_{min}$</td>
<td>The minimum computation bits requirement of the SN</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>The path loss factor</td>
</tr>
</tbody>
</table>

Fig. 2. The integrated BackCom and AC protocol in UC scenario.

In the UC scenario to avoid channel interference. Moreover, The channel is supposed to be quasi-static fading, which keeps unchange within $T$. We aim to maximize the user EE within $T$. The first time slot $t_0$ is the wireless energy transmission phase, the users can receive the RF signal from the HAP. After $t_0$, the SN can use the integrated BackCom and AC to offload tasks. During the last time slot, the HAP returns the computation results to the SN. Since the computation results are very small compared to the offloading tasks, we ignore the last time slot, e.g., $t_d \approx 0$.

C. Wireless Energy Transmission

Users harvest energy by the EH from the HAP during $t_0$. Then the SN and the helper transfer data in turns during the slots $t_{b, 0}^{h}$ and $t_{a, 0}^{h}$ by the BackCom. The SN can harvest energy from HAP in $t_{b}^{h}$ and the helper can harvest energy in $t_{a}^{h}$. So the harvested energy of the SN and the helper are

$$Q_{s} = \mu h_{s}(t_{0} + t_{b}^{h})P_{0},$$

and

$$Q_{h} = \mu h_{h}(t_{0} + t_{b}^{h})P_{0},$$

where $h_{s}$ and $h_{h}$ are the channel gain between the SN and the HAP, and the channel gain between the helper and the HAP, respectively. $P_0$ is the transmit power of the HAP, and $0 < \mu < 1$ denotes the energy conversion efficiency.

The task offloading can be executed in two ways, namely BackCom and AC. Let $l_{bac}^{s}, l_{b}^{h}, l_{act}^{p}, l_{a}^{p}$ and $l_{bac}^{p}$ denote the number
of tasks executed by the SN locally, offloaded to the helper by BackCom, offloaded to the HAP by BackCom, the offloading to the helper by the AC, and offloaded to the HAP by the AC, respectively.

D. Computation Model

1) Local Computing: The number of tasks executed locally at the SN is

\[ p_{loc}^s = \frac{f_s t_s}{\phi_s}, \]  

where \( \phi_s \) is the CPU cycles required to compute one bit task, \( t_s \) represents the local computing time and \( f_s \) denotes the local CPU frequency of the SN [31]. Meanwhile, the corresponding local computation energy consumption is

\[ E_{s}^{loc} = \kappa(f_s)^3 t_s, \]  

where \( \kappa \) is the effective capacitance coefficient, which depends on the circuit structure [32].

2) Offloading Tasks by BackCom: During \( t_{a}^b \), the SN can offload the \((l_{b}^h + p_{ap})\) data to the helper by the BackCom. \( l_{b}^h \) tasks will be transferred further to the HAP at \( t_{b}^h \). The remaining \( l_{b}^h \) tasks computed at the helper can be written as

\[ l_{b}^h = \frac{f_b t_{h1}}{\phi_h}, \]  

and the corresponding energy consumption is

\[ E_{h1}^{loc} = \kappa(f_h)^3 t_{h1}, \]  

where \( \phi_h \) is the CPU cycles at the helper required to compute one bit task, \( t_{h1} \) and \( f_h \) are the local computation time and the CPU frequency of the helper, respectively. It is worth noting that \( l_{b}^h \) bit data can be executed at the helper after the SN offloaded its partial tasks to the helper by the BackCom. Thus, we have this inequality \( 0 \leq t_{h1} \leq t_{b}^h + t_a \).

Denote \( \beta_s \) as the reflection coefficient of the SN, where \( 0 \leq \beta_s \leq 1 \). This means that the SN can divide the received signals into two parts: \( \beta_s \) part as carrier to transfer the data by the BackCom and \( 1 - \beta_s \) part of the harvesting energy [33]. Let \( W \) denote the WPMEC system bandwidth and \( g_0 \) denote the channel gain from the SN to the helper. The achievable task rate between the SN and the helper by the BackCom is expressed as \( r_{b}^s = W\log_2(1 + \frac{\zeta \phi h P_0 g_h g_0}{\sigma^2}) \), where \( \sigma^2 \) is the noise power and \( \zeta \) represents the performance gap reflecting the real modulation [34]. So the transmitted computation task during \( t_{b}^h \) is

\[ r_{b}^s t_{b}^h = t_{b}^h W\log_2 \left( 1 + \frac{\zeta \beta_s P_0 g_h g_0}{\sigma^2} \right), \]  

and we have \( l_{b}^h + p_{ap} \leq r_{b}^s t_{b}^h \). The circuit energy consumption of the SN can be expressed as

\[ E_{b}^{off} = p_{bac} r_{b}^s, \]  

and the harvested energy of the SN by the BackCom is

\[ Q_{b}^s = \mu h_s t_{b}^h P_0 (1 - \beta_s), \]  

where \( p_{bac} \) is the circuit power consumption of the SN by the BackCom.

During \( t_{a}^h \), the helper can offload the \( l_{a}^p \) data to the HAP by the BackCom. Let \( g_h \) represent the channel gain from the helper to the HAP. Therefore, the achievable task rate between the helper and the HAP by the BackCom is given by \( r_{a}^h = W\log_2(1 + \frac{\zeta_h \phi h P_h g_h g_0}{\sigma^2}) \), and \( 0 \leq \beta_h \leq 1 \) is the reflection coefficient of the helper. So the transmitted computation task during \( t_{a}^h \) is

\[ r_{a}^h t_{a}^h = t_{a}^h W\log_2 \left( 1 + \frac{\zeta_h \beta_h P_0 h_g g_h}{\sigma^2} \right). \]  

Therefore, we have \( l_{a}^p \leq r_{a}^h t_{a}^h \). The circuit energy consumption of the helper is

\[ E_{a}^{off} = p_{bac} t_{a}^h, \]  

and the harvested energy of the helper by the BackCom is

\[ Q_{a}^h = \mu h t_{a}^h P_0 (1 - \beta_h), \]  

where \( p_{bac} \) is the circuit power consumption of the helper by the BackCom.

3) Offloading Tasks by the AC: In addition to the BackCom, the task offloading can also use the AC mode. During the \( t_{a}^h \), the \((l_{a}^h + p_{ap})\) data can be offloaded to the helper by the AC. \( l_{a}^h \) tasks will be transferred further to the HAP at \( t_{a}^h \). The remaining \( l_{a}^h \) tasks computed at the helper can be written as

\[ l_{a}^h = \frac{f_a t_{h2}}{\phi_h}, \]  

and the corresponding energy consumption is

\[ E_{h2}^{loc} = \kappa(f_h)^3 t_{h2}, \]  

where \( t_{h2} \) is the local computation time of the helper, and \( 0 \leq t_{h2} \leq t_a \).

In addition, the channel capacity between the SN and the helper is expressed as \( r_{a}^s = W\log_2(1 + \frac{P_a g_0}{\sigma^2}) \), where \( P_a \) represents the transmit power of the SN. So the transmitted computation task is

\[ r_{a}^s t_{a}^h = t_{a}^h W\log_2 \left( 1 + \frac{P_a g_0}{\sigma^2} \right), \]  

and we have \( l_{a}^h + p_{ap} \leq r_{a}^s t_{a}^h \). The energy consumption of the SN is expressed as

\[ E_{a}^{off} = p_{bac} r_{a}^s + P_{bac} t_{a}^s, \]  

where \( P_{bac} \) is the circuit consumption of the SN by the AC.

During \( t_{b}^a \), the helper can offload the \( l_{a}^p \) data to the HAP by the AC. The channel capacity between the helper and the HAP is \( r_{b}^h = W\log_2(1 + \frac{P_b g_h g_0}{\sigma^2}) \), where \( P_b \) is the transmit power of the helper. Therefore, the maximum transmitted computation task is

\[ r_{a}^h t_{a}^h = W t_{a}^h \log_2 \left( 1 + \frac{P_b g_h g_0}{\sigma^2} \right), \]  

and we have \( l_{a}^p \leq r_{a}^h t_{a}^h \). The energy consumption of the helper is expressed as

\[ E_{a}^{off} = p_{bac} t_{a}^h + P_{bac} t_{a}^h, \]  

where \( P_{bac} \) is the circuit consumption of the helper by the AC.

Notice that the energy of the users is supplied from the HAP. So users are subject to the energy consumption constraints.
i.e., the total energy consumption cannot surpass the total harvested energy for each device. Specifically, we have

$$E_s^{loc} + E_s^{off} + E_a^{off} \leq Q_s + Q_h^s,$$

(19)

and

$$E_h^{loc} + E_h^{loc} + E_h^{off} + E_a^{off} \leq Q_h + Q_h^h.$$

(20)

III. PROBLEM FORMULATION AND THE OPTIMAL SOLUTION OF USER EE MAXIMIZATION PROBLEM

A. User EE Maximization Problem Formulation

In this section, we study the user EE maximization problem by jointly optimizing the system time allocation

$$t = \{t_0, t_b^h, t_a^h, t_a^b, t, t_{h1}, t_{h2}\},$$

resource allocation strategy

$$l = \{l_{s1}^b, l_{s1}^b, l_{s1}^a, l_{s1}^a, l_{s2}^b, l_{s2}^b, l_{s2}^a, l_{s2}^a\},$$

backscatter reflection coefficients

$$\beta = \{\beta_s, \beta_h\}$$

and power allocation

$$p = \{p_s, p_h\}.$$ Accordingly, the user EE maximization problem can be formulated as

$$P1:\ \max_{(t,l,p,\beta)} \frac{l_{total}}{E_{total}}$$

s.t. C1 : \(l_b^h + l_a^b \leq t_b^h W (\log_2 \left(1 + \frac{\zeta \beta_s p_0 h_s g_0}{\sigma^2}\right))\),

(21b)

C2 : \(l_a^h \leq t_a^h W (\log_2 \left(1 + \frac{\zeta \beta_s p_0 h_s g_h}{\sigma^2}\right))\),

(21c)

C3 : \(l_a^b + l_a^b \leq t_a^b W (\log_2 \left(1 + \frac{p g_h}{\sigma^2}\right))\),

(21d)

C4 : \(l_a^b \leq t_a^b W (\log_2 \left(1 + \frac{P h g_h}{\sigma^2}\right))\),

(21e)

C5 : \(0 \leq t_0 + t_b^h + t_a^b + t_a^a + t_h^h \leq T\),

(21f)

C6 : \(0 \leq t_s \leq T\),

(21g)

C7 : \(0 \leq t_{h1} \leq t_b^h + t_a^a \),

(21h)

C8 : \(t \geq 0\),

(21i)

C9 : \(0 \leq \beta_s \leq 1, 0 \leq \beta_h \leq 1\),

(21j)

C10 : \(l_{total} \geq L_{min}\),

(21k)

C11 : \((3),(5)\) and (13),

(21l)

C12 : \((19)\) and (20),

(21m)

where \(\eta_{EE}\) is the user EE, \(l_{total} = l_{total}^{loc} + l_{total}^{b} + l_{total}^{a} + l_{total}^{h} + l_{total}^{a}\) is total computation bits and \(E_{total} = E_s^{loc} + E_s^{off} + E_s^{off} + E_h^{loc} + E_h^{loc} + E_h^{off} + E_h^{off} + \mu h_s t_b^h P_0 \beta_s + \mu h_t t_b^h P_0 \beta_h\) is total energy consumption. C1-C4 represent the maximum transmitted computation bits by the BackCom and the AC. C5-C8 are the time allocation limits and C9 is the backscatter reflection coefficient constraint for the SN and the helper. C10 is the minimum computation bit requirement and C11 is the local computing relationship. C12 represents the energy consumption constraints. Due to the non-convex fractional objective function, non-convex constraints C1-C4 and the relationship of multivariate multiplication in C12, \(P1\) is a non-convex fractional optimization problem. In the following, we will convert \(P1\) into a convex optimization problem.

First of all, as for the fractional objective function, we apply the Dinkelbach method [36]. Specifically, let \(q'\) denote the optimal EE, \(q'\) is achieved if and only if this equation holds.

$$\max_{(t,l,p,\beta)} l_{total} - q' E_{total} = l_{total} - q' E_{total} = 0,$$

(22)

where \(\ast\) represents optimal solutions for all variables, \(l_{total}^\ast\) is the optimal computation bits and \(E_{total}^\ast\) is the optimal energy consumption. Thus, \(P1\) can be transformed to \(P2\) equivalently.

$$P2: \max_{(t,l,p,\beta)} l_{total} - q E_{total}$$

s.t. C1 : \((21b) - (21m)\)

(23a)

where \(q\) is a given parameter that should be determined afterward. However, because of the non-convex constraints \((23b)\), \(P2\) is more tractable than \(P1\). To deal with that, we introduce auxiliary variables \(\tau_s^b, \tau_h^b, \tau_s^a, \tau_h^a, \tau_s^b, \tau_h^b, \tau_s^a, \tau_h^a\), \(\tau_s^b\), and \(\tau_h^a\), where \(\tau_s^b = \beta_s t_b^h, \tau_h^b = \beta_h t_b^h, \tau_s^a = p_s t_a^a\), and \(\tau_h^a = p_h t_a^a\). By using these auxiliary variables, \(E_{total}\) can be converted to \(E_{total}'\), \(E_{total}' = E_s^{loc} + E_s^{off} + E_s^{off} + E_h^{loc} + E_h^{loc} + E_h^{off} + \mu h_s t_b^h \beta_s + \mu h_t t_b^h \beta_h \). According to \((21j)\), we have \(0 \leq \tau_s^b \leq t_b^h\) and \(0 \leq \tau_h^a \leq t_a^a\). Meanwhile, to simplify the mathematical expression, we introduce some constants \(A, B, C, D, E, F\), where \(\frac{\zeta h_s g_0}{\sigma^2}\) and \(\frac{g_h}{\sigma^2}\). Then, \(P2\) can be equivalently transformed into \(P3\).

$$P3: \max_{(t,l,p,\beta)} l_{total} - q E_{total}$$

s.t. C1 : \(t_b^h + l_a^b \leq t_b^h W (\log_2 \left(1 + \frac{\tau_s^b A}{t_b^h}\right))\)

(24a)

C2 : \(l_a^b \leq t_a^b W (\log_2 \left(1 + \frac{\tau_h^a}{t_b^h}\right))\)

(24b)

C3 : \(l_a^b \leq t_a^b W (\log_2 \left(1 + \frac{\tau_s^b}{t_a^h}\right))\)

(24c)

C4 : \(l_a^b \leq t_a^b W (\log_2 \left(1 + \frac{\tau_h^a}{t_a^b}\right))\)

(24d)

C5 : \(\kappa (f_s)^3 t_s + p^s t_b^h + P^s h t_a^a + \tau_a^a\)

(24e)

\(\leq \mu h_s (t_0 + t_b^h + t_a^h - \tau_s^b) P_0\),

(24f)

C6 : \(\kappa (f_h)^3 t_h^h + \kappa (f_h)^3 t_h^a + P^h h t_a^a + p^a h b_{bac} t_h^h + \mu \beta h (t_0 + t_b^h + t_a^h - \tau_h^a) P_0\)

(24g)

C7 : \(0 \leq \tau_s^b \leq t_b^h, 0 \leq \tau_h^a \leq t_a^a\)

(24h)

C8 : \((21f) - (21l)\)

(24i)
Algorithm 1: The User Energy Efficiency Maximization Algorithm.

Input: The channel gain, the system bandwidth, the nose power and other parameters in Table 2.

Initialize: The maximum iterations $I_{\text{max}}$, the error tolerance $\epsilon$ and initial EE $q = 0$.

for $i = 1 : I_{\text{max}}$ do
  cvx_begin
  Maximize $l_{\text{total}} - qE'_{\text{total}}$
  Subject to (24b)-(24i)
  cvx_end
  if $l_{\text{total}} - qE'_{\text{total}} < \epsilon$ then
    The optimal solution $\{t^*, \lambda^*, \tau^*\}$ are obtained, then calculate $\beta^*$ and $p^*$.
    Return optimal EE $q^*$ and break.
  else
    Update EE: $q = \frac{l_{\text{total}}}{E'_{\text{total}}}$.
  end
end

Output: Obtain the optimal resource allocation $\{t^*, \lambda^*, \beta^*, p^*\}$ and EE $q^*$ for $P1$.

Lemma 1. $P3$ is a convex optimization problem. It can be efficiently solved by convex optimization tools, such as CVX [37].

Proof. First, the constraints (24h) and (24i) are linear inequality constraints and linear equality constraints. Second, for (24b), $t^*_b Wlog_2(1 + \tau^*_b A)$ is the perspective of $Wlog_2(1 + \tau^*_b A)$, which is a concave function of $\tau^*_b$. Since the perspective operation preserves convexity [30], $t^*_b Wlog_2(1 + \tau^*_b A)$ is concave with respect to $\tau^*_b$ and $t^*_b$. It is obvious that $t^*_b + t_{\text{op}}^b$ is a linear function. Thus, the (24b) is a convex constraint. What’s more, for the energy constraint (24f), the right side is a linear function with respect to $t_s, t^*_b, t_{\text{op}}^b$ and $\tau^*_b$. The left side is also a linear function with regard to $t_a, t^*_a, t_{\text{op}}^a$ and $\tau^*_a$. So (24f) is also a convex constraint. Using the same analysis method for (24c)–(24e) and (24g), we can easily prove that these constraints are also convex constraints. Finally, by analyzing the above $l_{\text{total}}$ and $E'_{\text{total}}$, the objective function becomes a linear function after the EE $q$ is given. Thus, $P3$ is proved to be convex.

B. Optimal Solution for User EE Maximization Problem

In order to solve $P3$, an energy efficiency maximum algorithm is proposed in Algorithm 1. Besides, the Lagrange method can be employed to obtain some meaningful insights of the optimal solution.

Theorem 1. For the given non-negative Lagrange multipliers $\lambda_i, i = 1, 2, \ldots, 10$, the optimal backscatter reflection coefficients $\beta = \{\beta_s, \beta_h\}$ and the power allocation $p = \{p_s, p_h\}$ need to satisfy the following equations:

$$
\beta_s^* = \begin{cases}
0, & \text{if } t^*_b = 0 \\
\frac{\lambda_1 W}{((\lambda_5 - q)\mu h_a P_0 + \lambda_6)ln2 - \frac{\tau^*_b A}{\zeta P_0 h_s g_0}}, & \text{otherwise}
\end{cases}
$$

$$
\beta_h^* = \begin{cases}
0, & \text{if } t^*_b = 0 \\
\frac{\lambda_2 W}{((\lambda_6 - q)\mu h_a P_0 + \lambda_6)ln2 - \frac{\tau^*_b A}{\zeta P_0 h_s g_0}}, & \text{otherwise}
\end{cases}
$$

where $|x|^+ \triangleq \max\{0, x\}$.

Proof. Let $\lambda_i \geq 0 \forall i = 1, 2, \ldots, 10$ denote the Lagrange multipliers associated with the constraints (24b)–(24g), (21f) and (21k), respectively. The Lagrangian function of $P3$ is

$$
\mathcal{L} = l_{\text{total}} - qE'_{\text{total}} + \lambda_1 \left[ t^*_b + t_{\text{op}}^b - t^*_b Wlog_2 \left(1 + \frac{\tau^*_b A}{t^*_b}\right)\right] + \lambda_2 \left[ t_{\text{op}}^a - t^*_b Wlog_2 \left(1 + \frac{\tau^*_b B}{t^*_b}\right)\right] + \lambda_3 \left[ t^*_a + t_{\text{op}}^a - t^*_a Wlog_2 \left(1 + \frac{\tau^*_a C}{t^*_a}\right)\right] + \lambda_4 \left[ t_{\text{op}}^a - t^*_a Wlog_2 \left(1 + \frac{\tau^*_a D}{t^*_a}\right)\right] + \lambda_5 \left[ \kappa(f_s)^3 t_s + p_{\text{bac}}^s t^*_b + P_{\text{ttt}}^s t^*_a + \tau^*_b - \mu h_a (t_0 + t^*_b + t_{\text{op}}^b - \tau^*_b) P_0\right] + \lambda_6 \left[ \kappa(f_h)^3 t_h + \kappa(f_h)^3 t_h + P_{\text{ttt}}^h + p_{\text{bac}}^h + t^*_b - \tau^*_b P_0\right] + \lambda_7 \left[ t_0 + t^*_b + t_{\text{op}}^b + t^*_a - \tau^*_a - T\right] + \lambda_8 \left[ \tau^*_b - t^*_b + \lambda_9 \left[ t^*_b - t_{\text{op}}^b\right] + \lambda_{10} \left[ L_{\text{min}} - l_{\text{total}}\right]\right].
$$

We can use the first-order optimality condition. Let the gradients of the Lagrangian $\mathcal{L}$ with respect to $\tau^*_b, t^*_b, t^*_a$ and $t^*_a$ be zero, respectively.

$$
\tau^*_b = \frac{\lambda_1 W}{((\lambda_5 - q)\mu h_a P_0 + \lambda_6)ln2 - \frac{\tau^*_b A}{\zeta P_0 h_s g_0}},
$$

$$
\tau^*_a = \frac{\lambda_2 W}{((\lambda_6 - q)\mu h_a P_0 + \lambda_6)ln2 - \frac{\tau^*_a A}{\zeta P_0 h_s g_0}}.
$$
where \( |x|^{+} = \max\{0, x\} \). By using the relationships between these auxiliary variables and the original variables, we can easily obtain this theorem.

We can see from this theorem, when \( \zeta P_{0} h_{s} g_{0} \geq (\lambda_{s} - q) \ln 2 \sigma^{2} \), the SN is more willing to offload tasks by the BackCom. In other words, when the channel condition and the performance gap are good and the harvested energy is enough, the BackCom mode can be selected. In addition, when \( g_{0} \geq (\lambda_{s} - q) \ln 2 \sigma^{2} \), e.g., the channel condition between the SN and the helper is well, the SN will choose the AC mode. As for the helper, we can also draw the same conclusions.

IV. SIMULATION RESULTS

In this section, some numerical results are provided to evaluate the performance of the proposed cooperation-assisted WPMEC with the integrated BackCom and AC scheme, compared with the following four schemes.

A. User Cooperation With AC Scheme

In this scheme, users utilize the traditional harvest-then-offloading protocol to accomplish the computation tasks. Specially, the SN and the helper first harvest energy from the HAP, and then the SN utilizes the harvested energy to accomplish the computation tasks with the aid of the helper and the HAP. During this process, all task offloading can only use the AC, and the BackCom is banned. Thus, we can easily set \( t_{b} = 0 \) and \( t_{a} = 0 \) in \( P1 \) to achieve this scheme.

B. User Cooperation With BackCom Scheme

In this scheme, users utilize the BackCom mode to accomplish the computation tasks. Specially, the HAP broadcasts energy to users during a whole time block \( T \). The SN can also accomplish computation tasks with the aid of the helper and the HAP. However, all task offloading can only use the BackCom, and the AC is banned. Thus, users need to adjust the backscatter reflection coefficient to maintain the basic circuit consumption and achieve data transformation. We can easily set \( t_{0} = 0 \) and \( t_{a} = 1 \) in \( P1 \) to achieve this scheme.

C. Without User Cooperation With Integrated BackCom and AC Scheme

In this scheme, the SN directly communicates with the HAP without the aid of the helper. Specially, it first harvests the energy from the HAP and then can offload tasks to the HAP by the integrated the BackCom and AC. Owing to the bad channel condition between the SN and the HAP, it may harvest less energy and offload a little part of tasks to the HAP. In addition, it can accomplish its computation tasks by local computing during the entire time block \( T \).

D. Throughput Maximization in User Cooperation With Integrated BackCom and AC Scheme

In this scheme, we maximize the total computation bits \( l_{total} \) under the same condition of \( P1 \). Compared with the proposed scheme, this scheme can exhaust the remaining energy to get the maximum computation rates, so the energy utilization is low.

In this simulation, we set the communication channel to \( d^{-\alpha} \), where \( d \) denotes the distance between different devices, \( \alpha \) is the path-loss exponent. The distances between the SN and the helper, between the SN and the HAP and between the helper and the HAP are 12 m, 30 m and 20 m, respectively. The details of other parameters are exhibited in Table II.

Fig. 3 illustrates the user EE versus the performance gap \( \zeta \). As is illustrated, it obviously shows that the EE increases as the performance gap increases in the BackCom scheme and the integrated BackCom and AC scheme while the AC scheme remains unchangeable. The proposed scheme can achieve the best system performance, because it can make a full use of advantages of the BackCom and the AC. When \( \zeta > -16 \) dB, the BackCom scheme outperforms the AC scheme, so the proposed

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>The time block ( T )</td>
<td>1 s</td>
</tr>
<tr>
<td>The power of the HAP ( P_{0} )</td>
<td>4 W</td>
</tr>
<tr>
<td>The noise power ( \sigma^{2} )</td>
<td>( 10^{-10} ) W</td>
</tr>
<tr>
<td>The system bandwidth ( W )</td>
<td>1 MHz</td>
</tr>
<tr>
<td>The circuit consumption of the BackCom ( p_{b}^{\text{bac}} ) and ( p_{h}^{\text{bac}} )</td>
<td>1 ( \mu W )</td>
</tr>
<tr>
<td>The circuit consumption of the AC ( p_{s}^{\text{bac}} ) and ( p_{h}^{\text{bac}} )</td>
<td>10 ( \mu W )</td>
</tr>
<tr>
<td>The minimum computation bits requirement of the SN ( L_{\text{min}} )</td>
<td>10 bit</td>
</tr>
<tr>
<td>The CPU cycles required to compute 1 bit task ( \phi_{s} )</td>
<td>1500</td>
</tr>
<tr>
<td>The CPU cycles required to compute 1 bit task ( \phi_{h} )</td>
<td>1000</td>
</tr>
<tr>
<td>The CPU frequency of the SN ( f_{s} )</td>
<td>0.2 GHz</td>
</tr>
<tr>
<td>The CPU frequency of the helper ( f_{h} )</td>
<td>0.4 GHz</td>
</tr>
<tr>
<td>The path loss factor between the SN and the HAP ( \alpha_{0} )</td>
<td>3.5</td>
</tr>
<tr>
<td>The path loss factor between the helper and the HAP ( \alpha_{1} )</td>
<td>2.6</td>
</tr>
<tr>
<td>The path loss factor between the SN and the helper ( \alpha_{2} )</td>
<td>2.6</td>
</tr>
<tr>
<td>The equal computing efficiency parameter ( \kappa )</td>
<td>( 10^{-29} )</td>
</tr>
<tr>
<td>The energy conversion efficiency coefficient ( \eta )</td>
<td>0.7</td>
</tr>
<tr>
<td>The maximum iterations ( I_{\text{max}} )</td>
<td>10</td>
</tr>
<tr>
<td>The error tolerance ( \epsilon )</td>
<td>( 10^{-10} )</td>
</tr>
</tbody>
</table>
scheme can allocate more time to the BackCom mode. When \( \zeta < -22 \) dB, the proposed scheme nearly works on the AC mode. Thus, we can conclude that the proposed scheme is more flexible than other schemes.

Fig. 4 shows that the user EE versus the number of iterations. We can see from Fig. 4 that after five iterations, our proposed algorithm can converge to the optimal EE under different circuit consumption of the BackCom, which proves that our algorithm is computation-effective. Besides, the user EE decreases with the increase of \( p_{bac}^h \) and \( p_{bac}^s \). Obviously, for the same computation rate, the larger the circuit consumption of the BackCom, the more energy can be consumed.

Fig. 5 shows that the user EE versus different schemes, where \( \zeta = -17 \) dB. It is worth noting that the proposed scheme can achieve the best EE among all five schemes, which illustrates the advantages of the integrated BackCom and AC. In addition, the without-user-cooperation scheme with the integrated BackCom and AC has the lower EE. Even though using the integrated BackCom and AC mode, the terrible channel condition between the SN and the HAP still brings about less harvested energy and offloading tasks. This explains the importance of the UC for improve the property of the far user. It can be observed that the throughput maximization scheme is the lowest EE, so setting the EE as the objective function can achieve a higher energy utilization.

In Fig. 6, we plot the relationship between the optimal time allocation \( t^* \) and the performance gap \( \zeta \). As desired, when \( \zeta \) is small, the BackCom mode cannot achieve larger computation bits compared with the consumed energy, so users are willing to allocate more time \( t^*_0 \) to harvest the energy and then use the AC mode to offload the tasks. In addition, \( t^*_0 \) decreases with the increase of \( \zeta \) and when \( \zeta \geq -22 \) dB, \( t^*_0 \approx 0 \). The reason is that the BackCom mode can achieve more computation bits with the increase of \( \zeta \) under the same energy consumption, so the BackCom mode becomes more energy efficiency for users. The BackCom mode can be chosen to reflect the incident signal to transmit tasks and collect energy simultaneously to support the circuit consumption [38]. Thus, \( t^*_a \) and \( t^*_b \) increase while \( t^*_c \) and \( t^*_h \) decrease with the increase of \( \zeta \).

Fig. 7 shows the user EE versus the minimum computation bits requirement. Obviously, each user EE of the other three schemes decrease as the minimum computation bits requirement
$L_{\text{min}}$ increases except the throughput maximization scheme. The reason is that with $L_{\text{min}}$ increases, more system resources can be provided to satisfy the minimum computation bits requirement, which leads to consuming much more energy. In the throughput maximization scheme, the objective function is to maximize the computation bits. Within a certain range of $L_{\text{min}}$, it can meet the requirement. Thus, the EE of this scheme keeps unchanged at a very low EE. Besides, our proposed scheme can achieve maximum EE than other schemes, which also shows the advantages of the UC scheme with the integrated BackCom and AC.

V. CONCLUSION

In this article, we investigated an innovative cooperation-assisted WPMEC system with the integrated BackCom and AC, where we formulated a problem of maximizing the user EE by jointly optimizing the backscatter reflection coefficient for the BackCom, the transmission power for the AC, the time and task allocation when considering the minimum computation bits requirement, the channel capacity and the energy constraint. The integrated BackCom and AC protocol based on TDMA in the UC scenario was proposed to avoid interference. Based on the variable substitution, the fractional program and convex optimization techniques, we transformed the original problem into a convex optimization problem and obtained the semi-closed form of an optimal solution. An energy efficiency maximization algorithm was proposed to solve this convex optimization problem. Simulation results showed that the proposed scheme outperforms existing schemes in maximizing the user EE, which demonstrated the advantages of our proposed scheme.

REFERENCES

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